

HINTS & SOLUTIONS

Atomic Structure

[Set-1]

SECTION-A

1. (ii): $r_n = \frac{0.529}{Z} n^2$

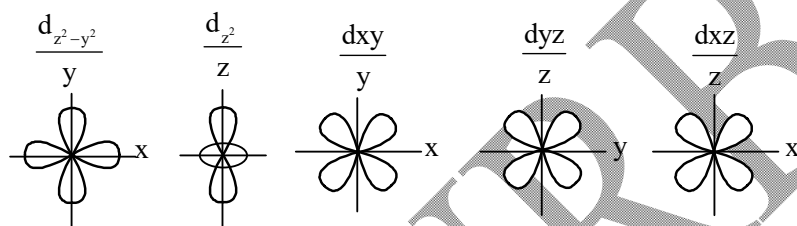
$$r_n = \frac{n^2}{Z} r_H$$

$$r_n = r_H \text{ only where } n = 2, Z = 2$$

i.e., Be^{3+}

2. (ii): In order to have least energetic photon electron should make a transition from $n = 5$ to $n = 4$.

3. (i):



4. (iii): $2p_x$, $2p_y$ and $2p_z$ all three have the same size, same shape and same energy but have different orientation in space.

5. (iii): Photon $\rightarrow$ shown dual nature, both momentum and wavelength

Electron $\rightarrow$ probability density

$\psi^2 \rightarrow$ always positive

$n \rightarrow n = 1 \rightarrow$ K-shell, $n = 2$, L shell

$n = 4$, N-shell

6. (iv): For f-subshell, $l = 3$

$\therefore m = (2l + 1)$, $m = (2 \times 3 + 1) = 7$, there are seven f-orbitals.

7. (i): Orbital angular momentum depends only on the azimuthal quantum number

$$L = \sqrt{\ell(\ell + 1)} \frac{h}{2\pi}$$

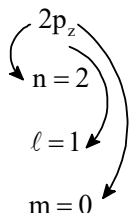
For $4p$, as well as for $3p$, $l = 1$

$\therefore L$ will be same.

8. (ii) For H-atom, energy depends only on the principal quantum number.

3s ($n = 3$) has a higher energy than 2p ($n = 2$)

9. (iv):



10. (iii):

$_{17}\text{Cl}^-$	$1s^2$	$2s^2$	$2p_x^2$	$2p_y^2$	$2p_z^2$	$3s^2$	$3p_x^2$	$3p_y^2$	$3p_z^2$
$n = 1$	1	2	2	2	2	3	3	3	3
$l =$	0	0	1	1	1	0	1	1	1
$n + l$	1	2	3	3	3	3	4	4	4

8 electron in Cl^- will have $n + l = 3$

11. Wave number of the longest wavelength transition in the Balmer series for H-atom is with minimum energy.

This is when $n_L = 2$, $n_H = 3$

$$\bar{\nu} = 1.097 \times 10^7 \left(\frac{1}{n_L^2} - \frac{1}{n_H^2} \right) \text{m}^{-1}$$

$$\bar{\nu} = 1.097 \times 10^7 \left(\frac{1}{2^2} - \frac{1}{3^2} \right) = 1.097 \times 10^7 \times \frac{5}{36}$$

$$\bar{\nu} = 1.52 \times 10^6 \text{ m}^{-1}$$

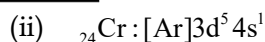
OR

$$(i) \quad r_2 = \frac{n^2}{Z} \times 0.259 = \frac{(2)^2}{2} \times 0.529$$

$$r_{2(\text{He}^+)} = 1.058 \text{ \AA}$$

$$(ii) \quad \frac{1}{2} \text{ (half)}$$

12. (i) $_{29}\text{Cu}^{2+} : [\text{Ar}]3d^9$



Both the species have unpaired electron present, hence both are paramagnetic and attracted towards the magnetic field.

13. $\text{K.E} = 4.55 \times 10^{-19} = \frac{mv^2}{2}$

$$v^2 = \frac{4.55 \times 10^{-19} \times 2}{9.1 \times 10^{-31}} = 10^{12}$$

$$v = 10^6 \text{ m/s}$$

$$\lambda = \frac{h}{mv} = \frac{6.62 \times 10^{-34}}{9.1 \times 10^{-31} \times 10^6}$$

$$\lambda = 7.27 \times 10^{-10} \text{ m}$$

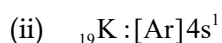
14. (i) **Pauli exclusion principle** states that “no two electrons in an atom can have the same set of four quantum numbers”

(ii) For 3p, $n = 3, l = 1$

(iii) For $n = 4, l = 2 \rightarrow 4d$, can accommodate maximum five electrons with $m_s = +\frac{1}{2}$

OR

(i) **Hund's rule of maximum multiplicity** states that “no pairing of electrons starts in the degenerate atomic orbitals until and unless each one is singly filled”



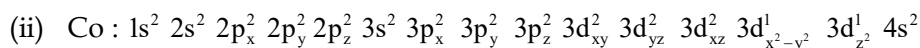
The highest energy electron is in 4s. The four quantum number are

$$n = 4, l = 0, m = 0, m_s = +\frac{1}{2}$$

15. (i) 4p

$$\text{Radial nodes} = n - l - 1 = 4 - 1 - 1 = 2$$

$$\text{Angular nodes } l = 1$$



No. of orbital filled with one or more electrons equals to 15.

(iii) $m = 100 \text{ g} = 0.1 \text{ kg}$

$$\Delta v = 50 \text{ m/s}$$

$$\Delta x \cdot m \Delta v \geq \frac{h}{4\pi}$$

$$\Delta x = \frac{h}{4\pi m \Delta v} = \frac{6.62 \times 10^{-34}}{4 \times 3.14 \times 0.1 \times 50}$$

$$\Delta x = 1.054 \times 10^{-35} \text{ m}$$

OR

$$mvr = n \frac{h}{2\pi} \quad \dots(i) \text{ (Bohr postulate)}$$

m = mass of an electron

v = speed of electron

r = radius of an orbit

$$2\pi r = n \frac{h}{mv}$$

But $\frac{h}{mv} = \lambda$ (de-Broglie equation)

$$\therefore \boxed{2\pi r = n\lambda}$$

(ii) Electron is a microscopic particle, continuously in motion. Electron shows more of wave nature. Hence, the exact path of an electron cannot be traced around the nucleus.

(iii) $n_L = 2$ $n_H = 4$

$$\Delta E = 2.18 \times 10^{-18} (1)^2 \left[\frac{1}{2^2} - \frac{1}{4^2} \right] = 2.18 \times 10^{-18} \times \frac{3}{16}$$

$$\Delta E = 4.0875 \times 10^{-19} \text{ J}$$