

HINTS & SOLUTIONS

Atomic Structure

[Set-2]

SECTION-A

1. (iii): $\Delta E = \frac{hc}{\lambda} = 2.18 \times 10^{-18} Z^2 \left[\frac{1}{n_L^2} - \frac{1}{n_H^2} \right] \text{ J}$

2. (ii): $E_1 = \frac{hc}{\lambda_1} \quad E_2 = \frac{hc}{\lambda_2}$

$$\frac{E_1}{E_2} = \frac{\lambda_2}{\lambda_1}$$

$$\lambda_1 = \lambda_2 \frac{E_2}{E_1} = \lambda_2 \frac{50}{25}$$

$$\boxed{\lambda_1 = 2\lambda_2}$$

3. (iv): For d-electron, $l = 2$

$$L = \sqrt{\ell(\ell+1)} \frac{h}{2\pi} = \sqrt{2(2+1)} \frac{h}{2\pi}$$

$$L = \sqrt{6} \frac{h}{2\pi}$$

4. (iii): $\Delta x = \Delta p$

$$\therefore \Delta x \cdot \Delta p = \frac{h}{4\pi}$$

$$(\Delta p)^2 = \frac{h}{4\pi}$$

$$(m\Delta v)^2 = \frac{h}{4\pi}$$

$$v^2 = \frac{h}{m^2 4\pi}$$

$$\Delta v = \frac{1}{2m} \sqrt{\frac{h}{\pi}}$$

5. (ii): $n \rightarrow$ size and energy of orbital

$$l \rightarrow \text{shape of orbital}$$

$$m \rightarrow \text{orientation of orbital}$$

$$m_s \rightarrow \text{spin of electron}$$

6. (i): ${}_{19}\text{K}: [\text{Ar}](4s^1) \rightarrow$ This is the electron with highest energy is K

$(n + l)$ for $4s = 4$ and $(n + l)$ value of $3d$ is 5.

7. (ii): 1st line in the Lyman series will require the minimum energy and maximum wavelength. The maximum wavelength of the limiting line is

$$\frac{1}{\lambda} = 1.097 \times 10^7 \left[\frac{1}{1^2} - \frac{1}{\infty^2} \right] = 1.097 \times 10^7 \text{ m}^{-1}$$

$$\lambda = \frac{1}{1.097 \times 10^7}$$

$$\lambda = 0.911 \times 10^{-7} \text{ m}$$

$$\lambda = 91.1 \text{ nm}$$

8. (i): For s-orbital, orbital angular momentum, L is zero means, the probability of finding electrons is same in all directions.

9. (iii): Total number of nodes = $n - 1$

For $3d$, no. of nodes = $3 - 1 = 2$

For $4f$, no. of nodes = $4 - 1 = 3$

10. (iv): Number of radial nodes $n - l - 1$

For $2p_x, 2p_y, 2p_z$, $n = 2, l = 1$

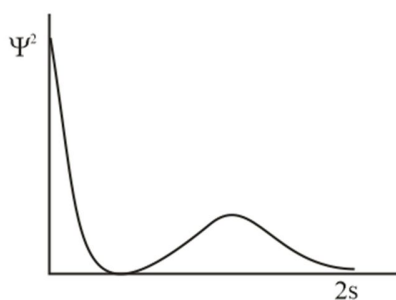
$\therefore$ number of radial nodes = $2 - 1 - 1 = 0$

11. (i) This is a violation of Hund's rule which states that "no pairing of electrons starts in the degenerate atomic orbital until and unless each one is singly filled".

- (ii) ψ^2 determines the probability of finding the electron in a given region in space.

12. (i) **Heisenberg's uncertainty principle** states that "it is impossible to determine the position and momentum of an object simultaneously with 100% accuracy".

- (ii)



OR

- (i) Einstein applied the Planck's quantum theory first in studying photoelectric effect.
 (ii) Two quantum numbers are required to define the subshell

Principal quantum number (n)

Azimuthal quantum number (l)

13. Second line in the Lyman series belongs to

$$n_L = 1 \longrightarrow n_H = 3$$

For He⁺

$$\frac{1}{\lambda} = 1.097 \times 10^7 (2)^2 \left[\frac{1}{1^2} - \frac{1}{3^2} \right]$$

$$= 1.097 \times 10^7 \times 4 \times \frac{8}{9}$$

$$\lambda = \frac{9}{1.097 \times 10^7 \times 4 \times 8} = 2.56 \times 10^{-8} \text{ m} = 256 \text{ \AA}$$

The spectral line falls in the UV region of the spectrum

OR

$$\lambda = 300 \text{ nm} = 3 \times 10^{-7} \text{ m} \quad \text{and} \quad E = 2 \text{ J}$$

$$E = N \frac{hc}{\lambda}$$

$$N = \text{number of photons} = \frac{E\lambda}{hc}$$

$$N = \frac{2 \times 3 \times 10^{-7}}{6.62 \times 10^{-34} \times 3 \times 10^8}$$

$$N = 3.0 \times 10^{18}$$

- 14.
- $m = 1 \text{ mg} = 10^{-3} \text{ g} = 10^{-6} \text{ kg}$

$$\Delta v = 5.5 \times 10^{-20} \text{ m/s}$$

$$\Delta x \cdot m \Delta v = \frac{h}{4\pi}$$

$$\Delta x = \frac{6.62 \times 10^{-34}}{4 \times 3.14 \times 10^{-6} \times 5.5 \times 10^{-20}}$$

$$\Delta x = 9.58 \times 10^{-10} \text{ m}$$

15. (i) $\lambda_A = 5 \times 10^{-8} \text{ m}$ $\lambda_B = ?$

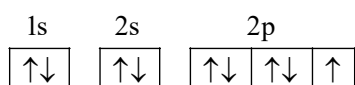
$$p_B = \frac{1}{2} p_A$$

$$\lambda = \frac{h}{p} \text{ (de-Broglie equation)}$$

$$\frac{\lambda_B}{\lambda_A} = \frac{p_A}{p_B} = 2$$

$$\lambda_B = 2\lambda_A = 2 \times 5 \times 10^{-8} = 10 \times 10^{-8} \text{ m}$$

(ii) $1s^2 2s^2 2p^5$



(iii) (a) 2s has lower energy than 2p due to low $(n + l)$ value

(b) $4d, n + l = 4 + 2 = 6$

$5f, n + l = 5 + 3 = 8$

4d has a lower energy than 5f.

OR

(i) (a) Principal quantum number (n) and azimuthal quantum number (l)

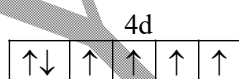
(b) Principal quantum number (n)

(c) Azimuthal quantum number (l)

(d) Magnetic quantum number (m)

(ii) $4d^6$

4d is a d-subshell in the 4th shell or 4th energy level containing six electrons, out of which four are unpaired



(iii) In H-atom, energy depend only on the principal quantum numbers.

(a) 3s has higher energy than 1s

(b) 3p has higher energy than 2p

(c) both will have same energy as n is same

(d) both will have same energy as n is same.